

Year 12 Mathematics Applications
Test 4 2017

Calculator Assumed
Finance

STUDENT'S NAME _____

DATE: Thursday 29th June

TIME: 50 minutes

MARKS: 51

INSTRUCTIONS:

Standard Items: Pens, pencils, drawing templates, eraser

Special Items: Three calculators, notes on one side of a single A4 page (these notes to be handed in with this assessment)

Questions or parts of questions worth more than 2 marks require working to be shown to receive full marks.

1. (9 marks)

Aaron is investigating obtaining a loan for a new car. Use the screen capture below to answer the following the questions regarding his loan.

(a) Fill in the blank spaces. [6]

A loan of _____, with an annual interest rate of _____, will be reduced to a balance of _____ after _____ years, when interest is compounded _____, i.e _____ times per year.

Compound Interest

| | |
|-----|--------------|
| N | 36 |
| I% | 7.8 |
| PV | 9100 |
| PMT | -350 |
| FV | -214.1490296 |
| P/Y | 4 |
| C/Y | 4 |

(b) Determine the interest rate per compounding period? [1]

(c) How much will Aaron's final repayment be? [2]

2. (3 marks)

Determine the principal that would need to be invested at 3.7% p.a. compounded daily to earn \$1400 interest in 6 years.

3. (5 marks)

Ryan would like to invest some money. By first determining the effective interest rate, rank the following options from the best (number 1) to the worst.

| Scheme | Effective Interest Rate | Rank |
|------------------------------------|--------------------------------|-------------|
| 10.5% p.a. compounding daily | | |
| 11% p.a. simple interest | | |
| 0.9% per month compounding monthly | | |

4. (9 marks)

Luke is depreciating his car for tax purposes. He can choose between using fixed depreciation at of \$2000 per year or reducing balance depreciation at rate of 15% per year. Luke purchased the car at the beginning of 2014 for \$38 000.

(a) Using the fixed depreciation method,

(i) determine the value of the car in 2017. [2]

(ii) after how many years will the value of the car first fall below \$15 000 [2]

(b) Using the reducing balance depreciation,

(i) write a recursive rule that gives the value of the car n years after 2014. [2]

(ii) determine the value of the car in 2017. [1]

(iii) after how many years will the value of the car first fall below \$15 000 [2]

5. (20 marks)

Liam is planning to borrow money from the bank to purchase a new car. He will get a reducible interest loan that compounds monthly and he will make regular monthly repayments.

The table below shows the progress for the first 6 months. All values have been rounded to the nearest cent.

| Month | Amount owing at the beginning of the month | Interest for the month | Repayment | Amount owing at the end of the month |
|-------|--|------------------------|-----------|--------------------------------------|
| 1 | \$ 25,000.00 | \$ 150.00 | \$ 700.00 | \$ 24,450.00 |
| 2 | \$ 24,450.00 | \$ 146.70 | \$ 700.00 | \$ 23,896.70 |
| 3 | \$ 23,896.70 | \$ 143.38 | \$ 700.00 | \$ 23,340.08 |
| 4 | \$ 23,340.08 | \$ 140.04 | \$ 700.00 | \$ 22,780.12 |
| 5 | \$ 22,780.12 | \$ 136.68 | \$ 700.00 | \$ 22,216.80 |
| 6 | \$ 22,216.80 | \$ 133.30 | \$ 700.00 | \$ 21,650.10 |
| 7 | | | | |

(a) Determine the values of **A**, **B**, **C** and **D** to complete the table below. [5]

| | |
|--------------------------|----------|
| Annual Interest Rate (%) | A |
| Number of compounds p.a | B |
| Monthly loan repayment | C |
| Starting amount | D |

(b) Complete the last row of the table, to show the progress for the 7th month. [2]

(c) In which month will Liam pay off the loan? [1]

(d) Determine the amount of interest that Liam will pay over the life of the loan. [3]

(e) What affect will it have on the loan if Liam repays \$150 per month? [2]

(f) Write a recurrence relation where V_n is the value outstanding after n months. [3]

After 2 years Liam explores some options to determine if he can pay the loan back quicker.

(g) If, after 2 years, Liam decides to double the repayment he makes each month, by how much will he shorten the life of the loan? [2]

(h) If Liam would like to repay the remaining amount in 6 equal monthly repayments, how much, to the nearest cent, should he repay each month? [2]

6. (5 marks)

To save up to buy a new car James opens a savings account that earns 11.4% p.a. compounded monthly. He initially deposits \$2700 when he opens the account at the beginning of the month and then he deposits \$420 at the end of every month.

(a) How much is in James' account after 2 years? [2]

(b) Calculate the interest earned in the two years as a percentage of James' total contributions to the account. [2]

(c) Explain why the percentage in part (b) is different from the annual interest rate. [1]